

ECE-223, Solutions for Assignment #2

Chapter 2, Digital Design, M. Mano, 3rd Edition

2.2)

Simplify the following Boolean expression to a minimum number literals:

- a) $xy + xy'$
- b) $(x + y)(x + y')$
- c) $xyz + x'y + xyz'$
- d) $(A+B)'(A'+B)'$

a) $xy + xy' = x(y+y') = x \cdot 1 = x$

b) $(x+y)(x+y') = xx + xy' + yx + yy' = x + xy' + xy + 0 = x(1 + y' + y) = x \cdot 1 = x$

Also $(x+y)(x+y') = x + yy' = x + 0 = x$

c) $xyz + x'y + xyz' = xy(z+z') + x'y = xy + x'y = y(x+x') = y$

d) $(A+B)'(A'+B)' = (A'B')(AB) = 0$

2.3)

Simplify the following Boolean expression to a minimum number literals:

- a) $ABC + A'B + ABC'$
- b) $x'yz + xz$
- c) $(x+y)'(x'+y')$
- d) $xy + x(wz + wz')$
- e) $(BC' + A'D)(AB' + CD')$

a) $ABC + A'B + ABC' = AB(C+C') + A'B = AB + A'B = B(A+A') = B$

b) $x'yz + xz = z(x'y+x) = z(x'+x)(x+y) = z(x+y)$

c) $(x+y)'(x'+y') = x'y' \cdot (x'+y') = x'y' + x'y' = x'y'$

d) $xy + x(wz + wz') = xy + xw(z+z') = xy + xw = x(y+w)$

e) $(BC' + A'D)(AB' + CD') = AB'BC' + AB'A'D + CD'BC' + CD'A'D = 0$

2.6)

Find the complement of the following expressions:

- a) $xy' + x'y$
- b) $(AB' + C)D' + E$
- c) $(x+y'+z)(x'+z')(x+y)$

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- a) $[xy' + x'y]' = (xy')' + (x'y)' = (x'+y).(x+y') = xx' + yy'$
b) $[(AB' + C)D' + E]' = [(AB' + C)D']'.E' = [(AB' + C)' + D].E' = [(A' + B).C' + D].E' = (A' + B + D).(C' + D).E'$
c) $[(x+y'+z)(x'+z')(x+y)]' = (x+y'+z)' + (x'+z')' + (x+y)' = x'yz' + xz + x'y'$
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2.7)

Given Boolean function F_1 and F_2 .

- a) Show that the Boolean function $E = F_1 + F_2$ contains the sum of the minterms of F_1 and F_2
b) Show that the Boolean function $G = F_1 \cdot F_2$ contains the sum of the minterms of F_1 and F_2

$$F_1 = \sum m_i \text{ and } F_2 = \sum m_j$$

a)
 $E = F_1 + F_2 = \sum m_i + \sum m_j = \sum (m_i + m_j)$

b)
 $G = F_1 F_2 = \sum m_i \cdot \sum m_j$
 $m_i \cdot m_j = 0 \text{ if } i \neq j$
 $m_i \cdot m_j = 1 \text{ if } i = j$

Therefore G has only common minterms.

2.14)

Obtain the truth table of the following functions and express each function in sum of minterms and product of maxterms:

- a) $(xy + z)(y + xz)$
b) $(A' + B)(B' + C)$
c) $y'z + wxy' + wxz' + w'x'z$

- a) $(xy + z)(y + xz) = xy + yz + xyz + xz = \sum(3, 5, 6, 7) = \prod(0, 1, 2, 4)$
b) $(A' + B)(B' + C) = A'B' + A'C + BC = \sum(0, 1, 3, 7) = \prod(2, 4, 5, 6)$
c) $y'z + wxy' + wxz' + w'x'z = \sum(1, 3, 5, 9, 12, 13, 14) = \prod(0, 2, 4, 6, 7, 8, 10, 11, 15)$
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2-15)

Given the Boolean function

- $F = xy'z + x'y'z + w'xy + wx'y + wxy$
a) Obtain the truth table of the function.
b) Draw the logic diagram using the original Boolean expression.

- c) Simplify the function to a minimum number of literals using Boolean algebra.
d) Obtain the truth table of the function from the simplified expression and show that it is the same as the one in part (a)
e) Draw the logic diagram from the simplified expression and compare the total number of gates with the diagram of part (b)

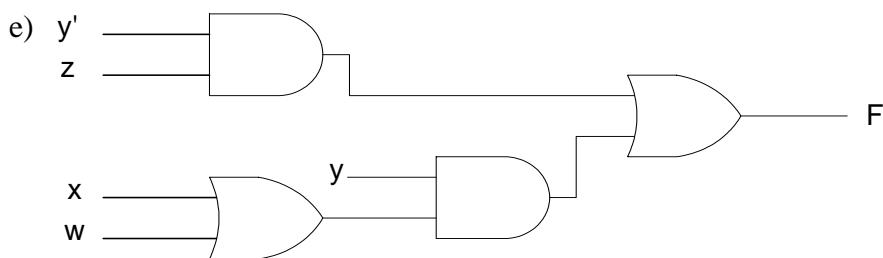
a) $F(w,x,y,z) = \sum(1,5,6,7,9,10,11,13,14,15)$

b) $F = xy'z + x'y'z + w'xy + wx'y + wxy$

5 3-input AND gate; 5 3-input OR gate

c) $F = y'z(x+x') + xy(w'+w) + wy(x'+x) = y'z + xy + wy = y'z + y(x+w)$

d) $F(w,x,y,z) = \sum(1,5,6,7,9,10,11,13,14,15)$



2.17)

Express the complement of the following function in sum of minterms:

a) $F(A,B,C,D) = \sum(0,2,6,11,13,14)$

b) $F(x,y,z) = \prod(0,3,6,7)$

a) $F'(A,B,C,D) = \sum(1,3,4,5,7,8,9,10,12,15)$

b) $F'(x,y,z) = \sum(0,3,6,7)$

2.18)

Convert the following to the other canonical form:

a) $F(x,y,z) = \sum(1,3,7)$

b) $F(A,B,C,D) = \prod(0,1,2,3,4,6,12)$

a) $F(x,y,z) = \sum(1,3,7) = \prod(0,2,4,5,6)$

b) $F(A,B,C,D) = \prod(0,1,2,3,4,6,12) = \sum(5,7,8,9,10,11,13,14,15)$

2.22)

By substituting the Boolean expression equivalent of the binary operation as defined in Table 2-8 (Digital Design, M. Mano, 3rd Edition,pp. 57) show the following:

- a) The inhibition operation is neither commutative nor associative.
- b) The exclusive-OR operation is commutative and associative.

a) $x/y = xy' \neq y/x = x'y$ Not Commutative
 $(x/y)/z = xy'z' \neq x/(y/z) = x(yz')' = xy' + xz$ Not Associative

b) $x \oplus y = xy' + x'y = y \oplus x = yx' + y'x$ Commutative
 $(x \oplus y) \oplus z = \sum(1,24,7) = x \oplus (y \oplus z)$ Associative